

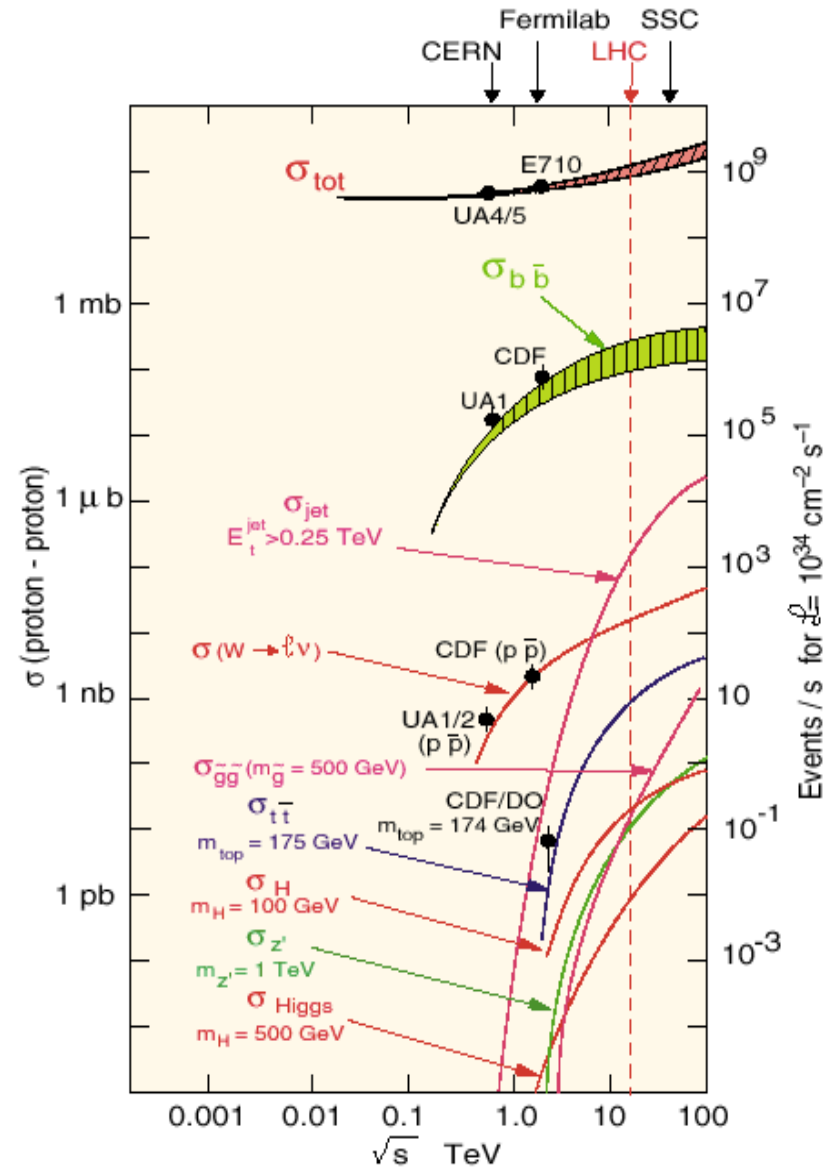
QUARKS, Валдай, 2018

The ODDERON: myths and reality

*(following the LHC (TOTEM) measurement of the real part
of the pp scattering amplitude at 13 TeV)*

László Jenkovszky (BITP, Kiev; jenk@bitp.kiev.ua)

- Total cross section at LHC
 $\sigma(\text{pp} \rightarrow \text{anything}) \sim 0.1 \text{ barn}$
- So a 1 pb Higgs cross section corresponds to one being *produced* every 10^{11} interactions!
 (further reduced by BR \times efficiency)
- Experiments have to be designed so that they can separate such a rare signal process from the background
- Rate = $L \cdot \sigma$
 where luminosity L (units $\text{cm}^{-2}\text{s}^{-1}$) is a measure of how intense the beams are
 LHC design luminosity = $10^{34} \text{ cm}^{-2}\text{s}^{-1}$



Observables:

- Elastic differential cross section:

$$\frac{d\sigma_{el}}{dt}(s, t) = \frac{\pi}{s^2} |A(s, t)|^2$$

- Total, (integrated) elastic and inelastic cross sections:

$$\sigma_{tot}(s) = \frac{4\pi}{s} \text{Im}A(s, t = 0)$$

$$\sigma_{el}(s) = \int_{t_{min}}^{t_{max}} \frac{\sigma_{el}(s, t)}{dt} dt$$

$$\sigma_{in}(s) = \sigma_{tot}(s) - \sigma_{el}(s)$$

- The (forward) phase, ρ :

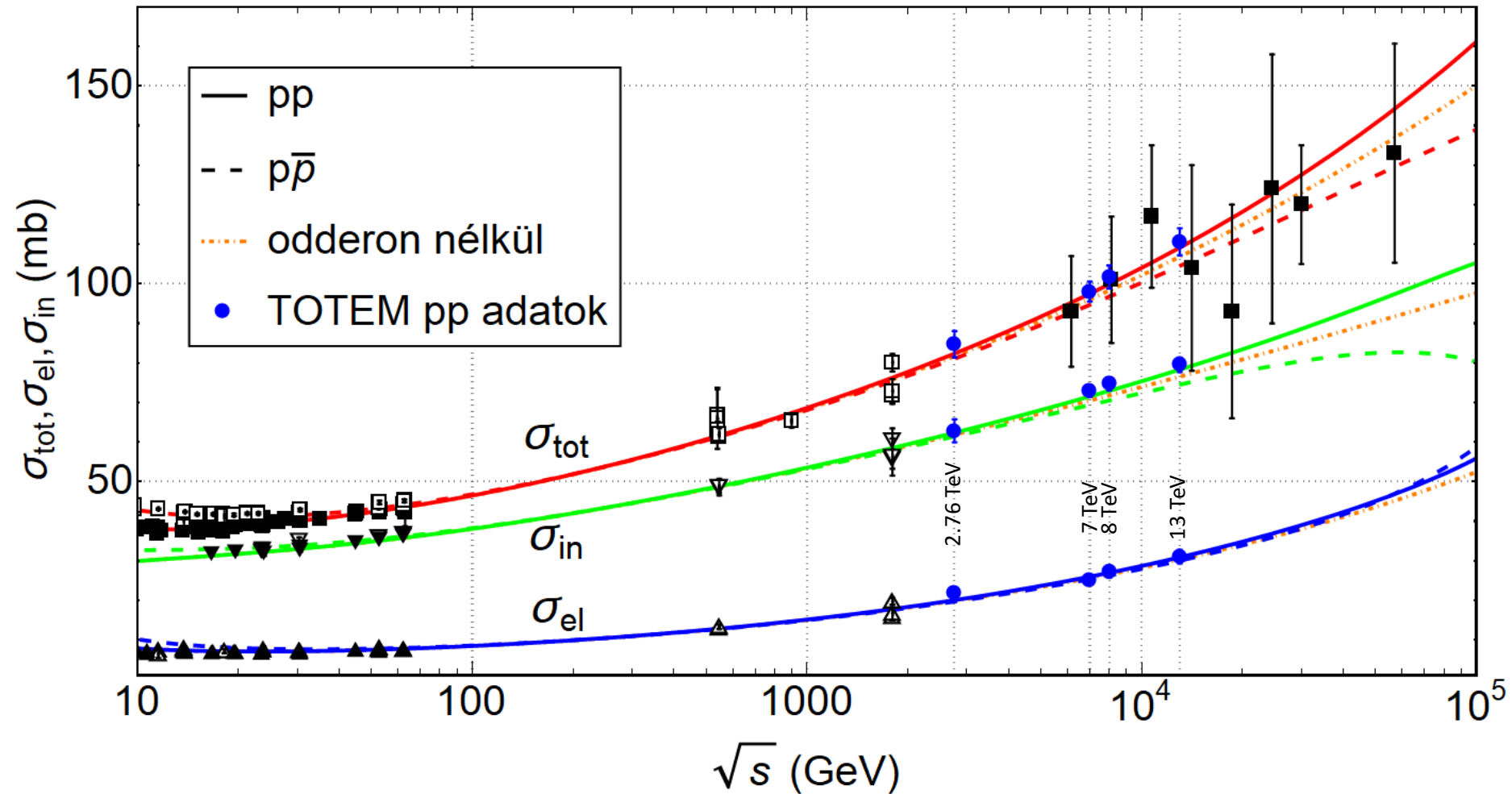
$$\rho(s) = \frac{\text{Re}A(s, t = 0)}{\text{Im}A(s, t = 0)}$$

- Slope of the (forward) slope ($B(s) \sim R^2(s)$):

$$B(s) = \frac{d}{dt} \left(\ln \frac{d\sigma_{el}}{dt}(s, t) \right) \Big|_{t=0}$$

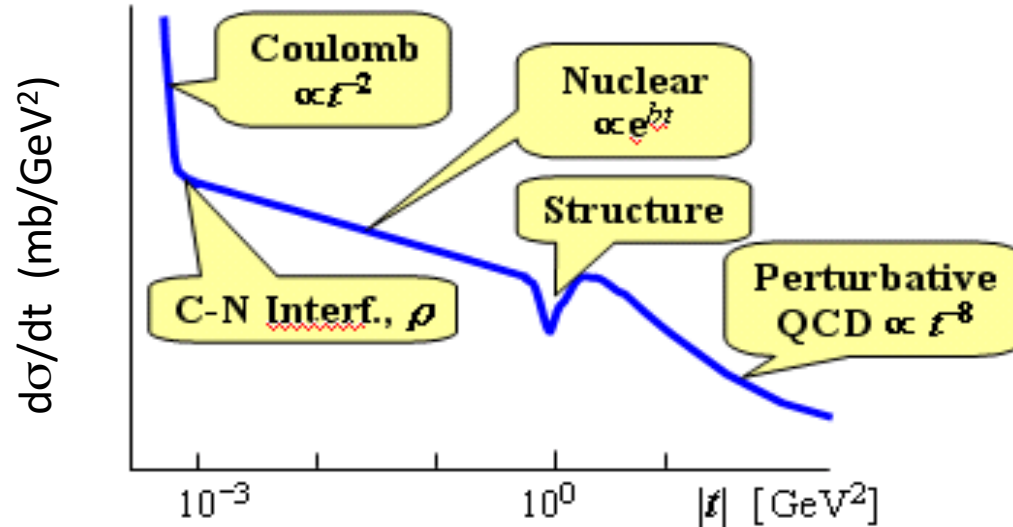
Total, elastic and inelastic cross-sections

- $30 \leq \sqrt{s} \leq 57000 \text{ GeV}$



Elastic Scattering

$\sqrt{s} = 14$ TeV prediction of BSW model



momentum transfer $-t \sim (p\theta)^2$
 θ = beam scattering angle
 p = beam momentum

$$\rho = \frac{\text{Re}(f_{el}(t))}{\text{Im}(f_{el}(t))} \Big|_{t \rightarrow 0}$$

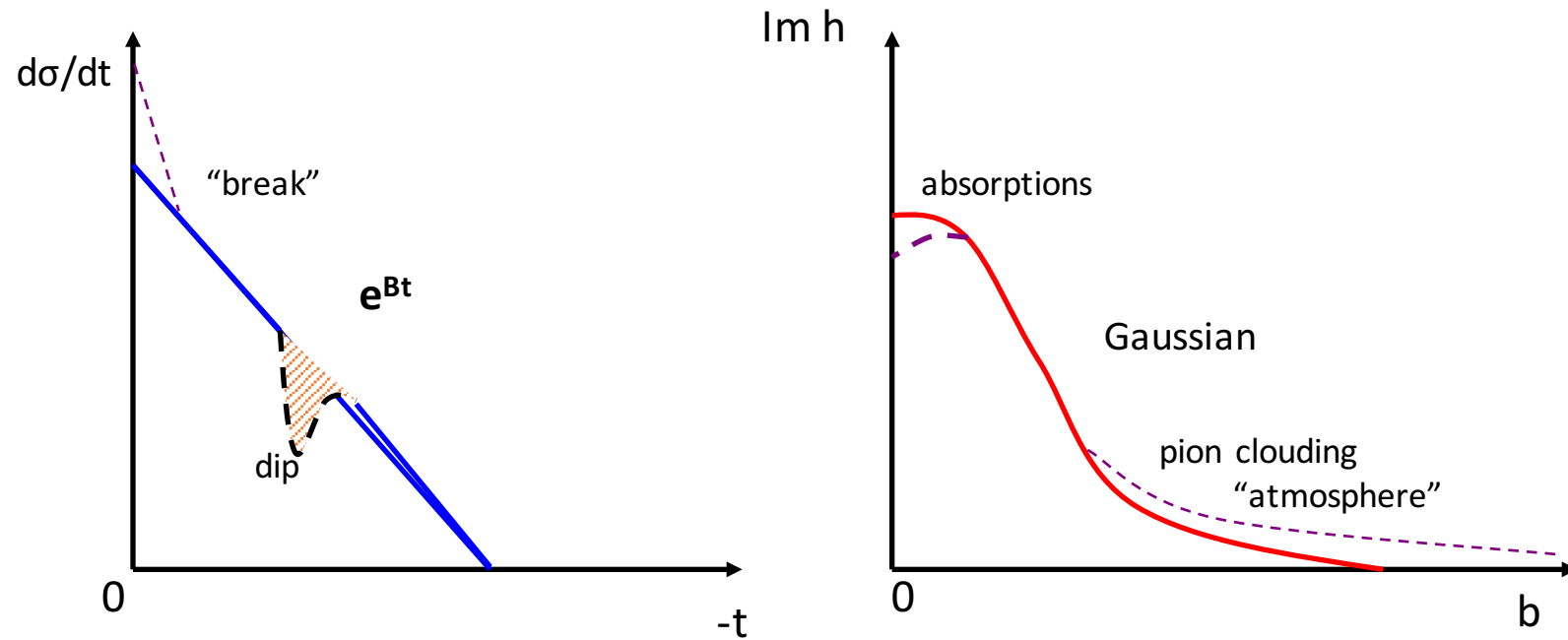
$$\left. \frac{dN}{dt} \right|_{t=CNI} = L\pi |f_C + f_N|^2 \approx L\pi \left| -\frac{2\alpha_{EM}}{|t|} + \frac{\sigma_{tot}}{4\pi} (i + \rho) e^{-\frac{b|t|}{2}} \right|^2$$

L , σ_{tot} , b , and ρ
 from FIT in CNI
 region (UA4)

CNI region: $|f_C| \sim |f_N| \rightarrow$ @ LHC: $-t \sim 6.5 \cdot 10^{-4} \text{ GeV}^2$; $\theta_{min} \sim 3.4 \text{ } \mu\text{rad}$

($\theta_{min} \sim 120 \text{ } \mu\text{rad}$ @ SPS)

1. On-shell (hadronic) reactions ($s, t, Q^2 = m^2$);
 $t \leftrightarrow b$ Fourier-Bessel transform dictionary:



7 TeV:

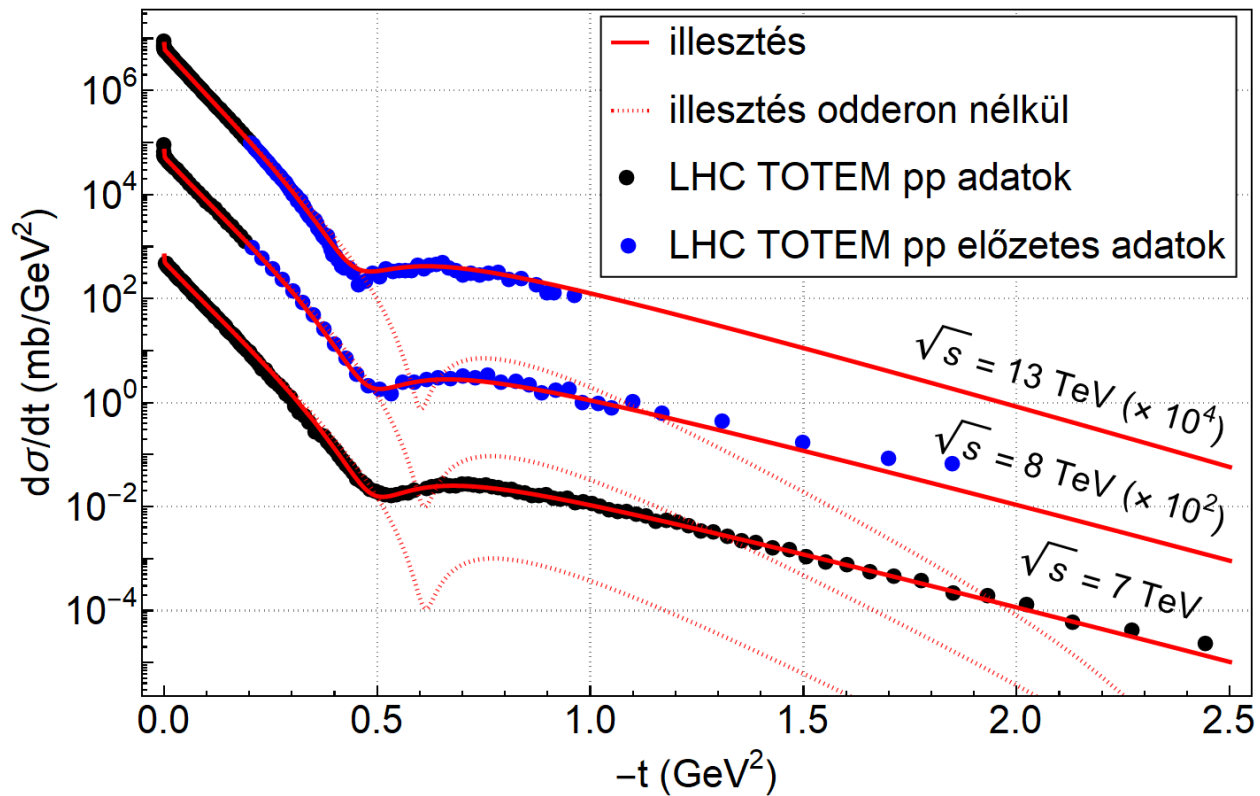
8 TeV:

13 TeV:

$0.35 \leq |t| \leq 2.5 \text{ GeV}^2$

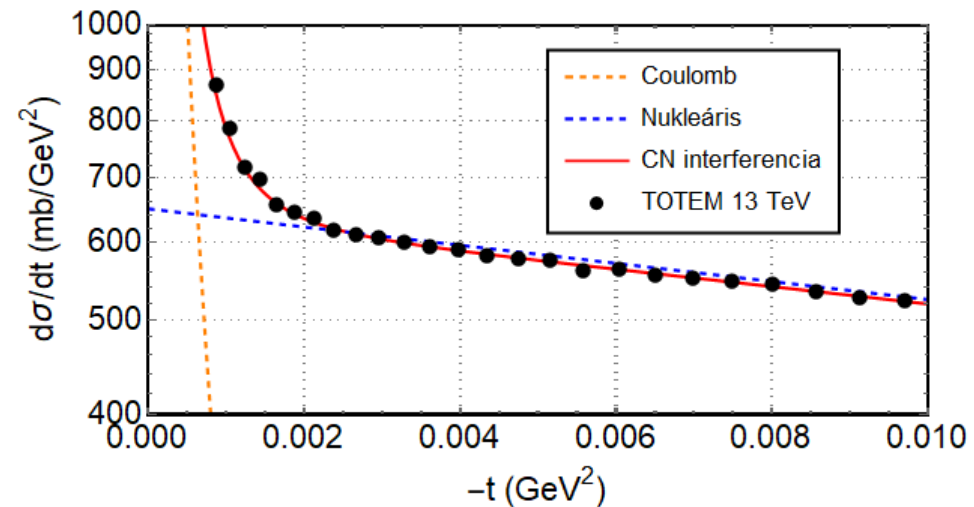
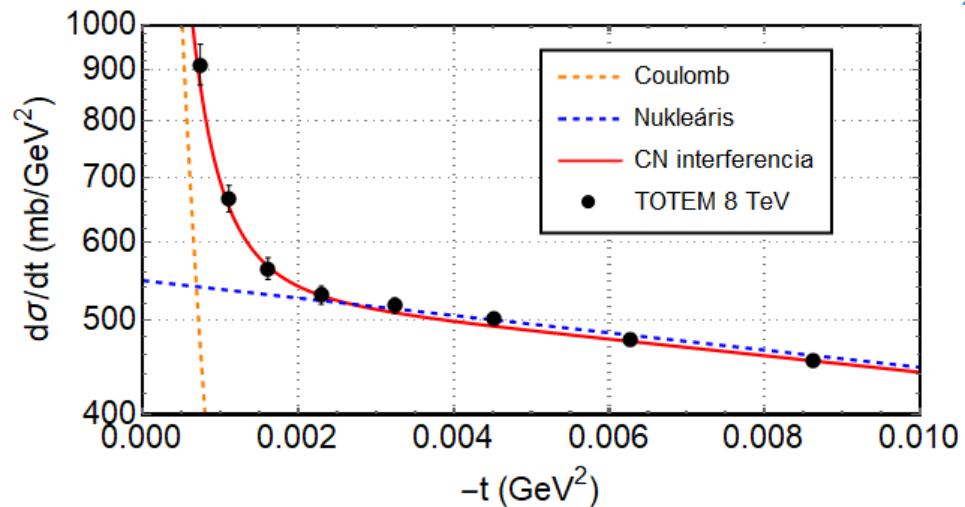
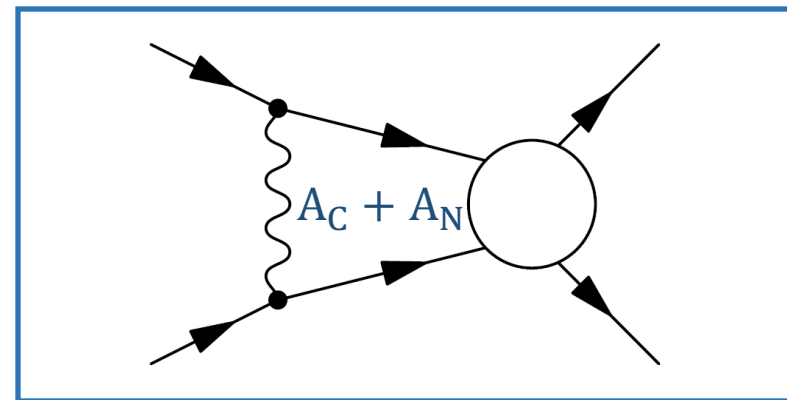
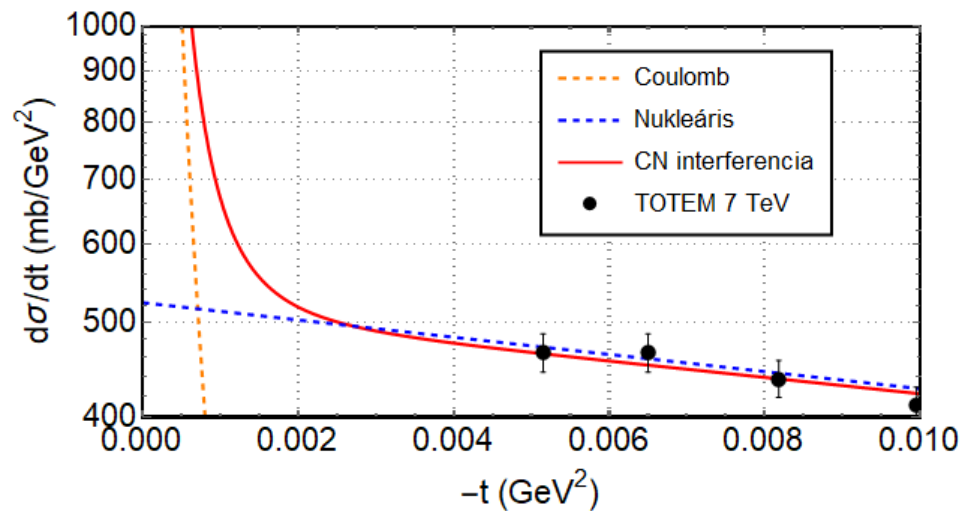
$0.0007 \leq |t| \leq 1.9 \text{ GeV}^2$

$0.0008 \leq |t| \leq 1 \text{ GeV}^2$



Szanyi I.: A rugalmas proton-proton szórás fizikai leírása

Coulomb-nuclear interference



f & ω reggeons:

$$A_{pp}^{p\bar{p}}(s, t) = A_f(s, t) \pm A_\omega(s, t) + A_P(s, t) \pm A_O(s, t)$$

$$A_f(s, t) = a_f e^{b_f t} e^{-\frac{i\pi\alpha_f}{2}} (s/s_{0f})^{\alpha_f}$$

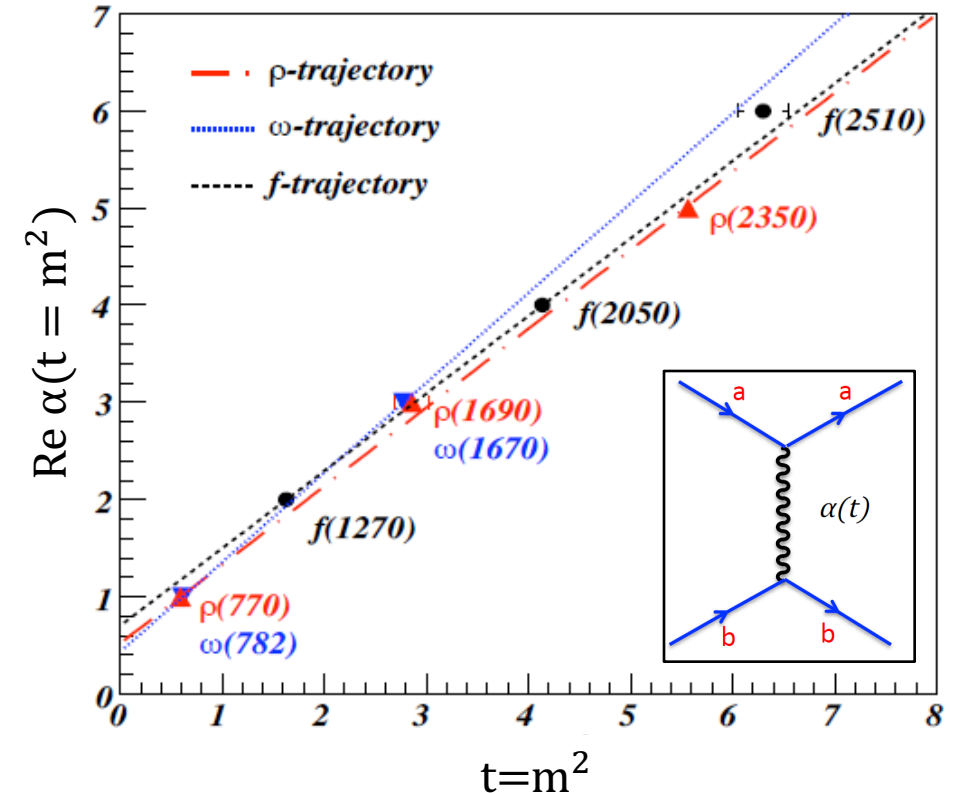
$$A_\omega(s, t) = ia_\omega e^{b_\omega t} e^{-\frac{i\pi\alpha_\omega}{2}} (s/s_{0\omega})^{\alpha_\omega}$$

$$\alpha_f \equiv \alpha_f(t) = 0.703 + 0.84t$$

$$\alpha_\omega \equiv \alpha_\omega(t) = 0.435 + 0.93t$$

Fitted parameters:

$$a_f, b_f, s_{0f}, a_\omega, b_\omega, s_{0\omega}$$



Chew-Frautschi plot.

Pomeron

$$A_{pp}^{p\bar{p}}(s, t) = A_f(s, t) \pm A_\omega(s, t) + A_P(s, t) \pm A_O(s, t)$$

- **Dipole Pomeron:**

$$A_P(s, t) = i \frac{a_P s}{b_P s_{0P}} [r_{1P}^2(s) e^{r_{1P}^2(s)[\alpha_P - 1]} - \varepsilon_P r_{2P}^2(s) e^{r_{2P}^2(s)[\alpha_P - 1]}]$$

$$r_{1P}^2(s) = b_P + L_P - i\pi/2$$

$$r_{2P}^2(s) = L_P - i\pi/2$$

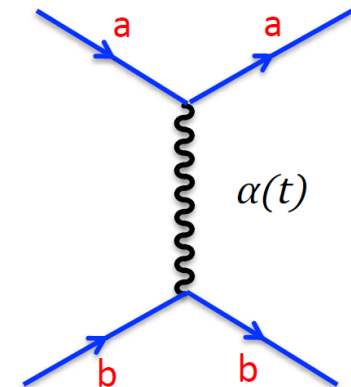
$$L_P \equiv \ln(s/s_{0P})$$

- **Pomeron trajectory:**

$$\alpha_P \equiv \alpha_P(t) = 1 + \delta_P + \alpha_{1P}t$$

- **Fitted paramers:**

$$a_P, b_P, \varepsilon_P, s_{0P}, \delta_P, \alpha_{1P}$$



Odderon

$$A_{pp}^{p\bar{p}}(s, t) = A_f(s, t) \pm A_\omega(s, t) + A_P(s, t) \pm A_O(s, t)$$

Odderon contribution:

$$A_O(s, t) = \frac{a_0 s}{b_0 s_{00}} [r_{10}^2(s) e^{r_{10}^2(s)[\alpha_0 - 1]} - \epsilon_0 r_{20}^2(s) e^{r_{20}^2(s)[\alpha_0 - 1]}]$$

$$r_{1P}^2(s) = b_0 + L_0 - i\pi/2$$

$$r_{20}^2(s) = L_0 - i\pi/2$$

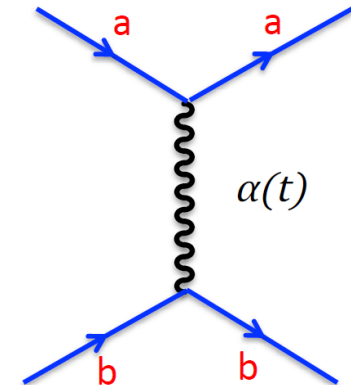
$$L_0 \equiv \ln(s/s_{00})$$

Odderon trajectory:

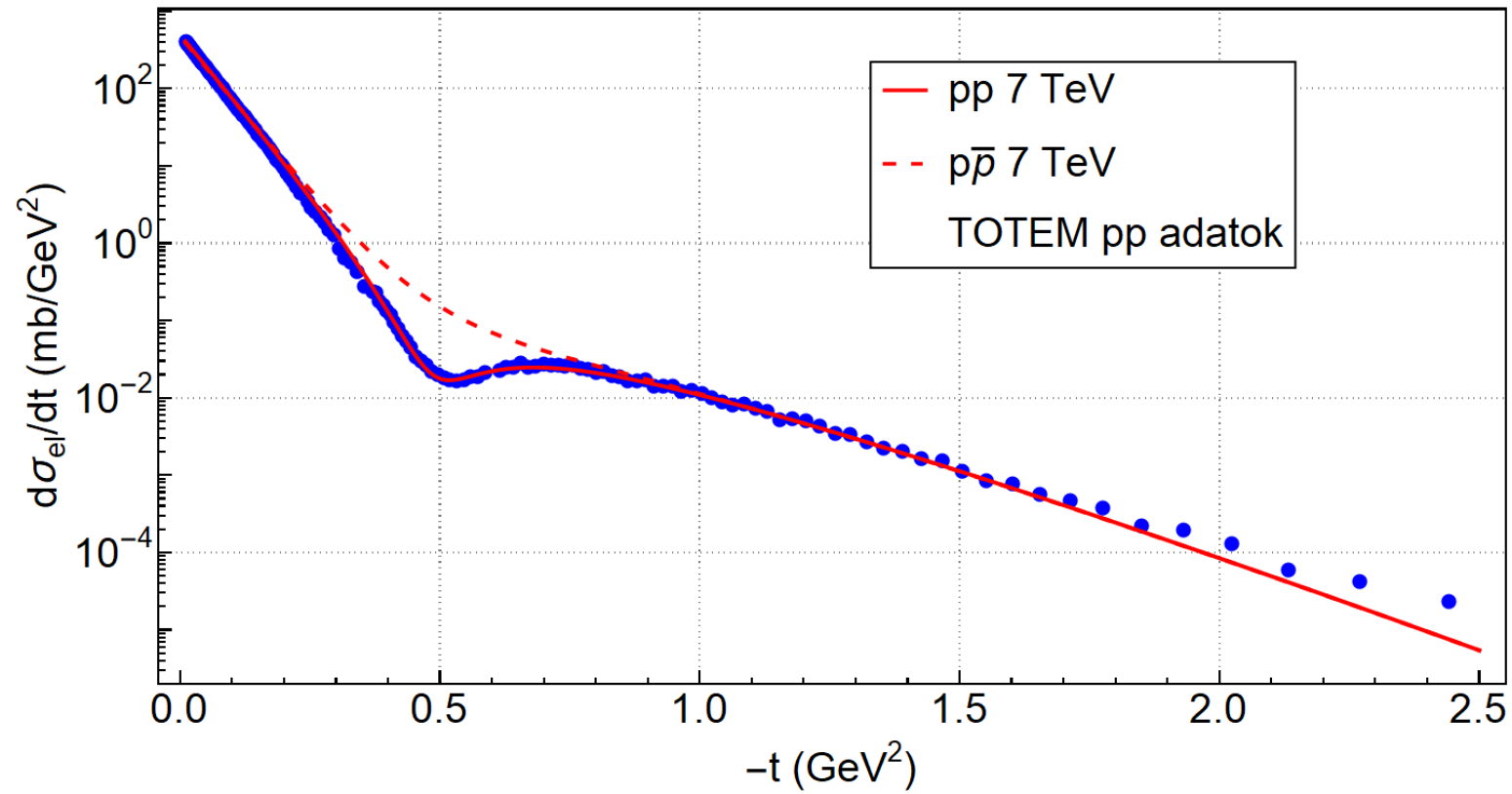
$$\alpha_O \equiv \alpha_O(t) = 1 + \delta_0 + \alpha_{10}t$$

Fitted parameters:

$$a_0, b_0, \epsilon_0, s_{00}, \delta_0, \alpha_{10}$$

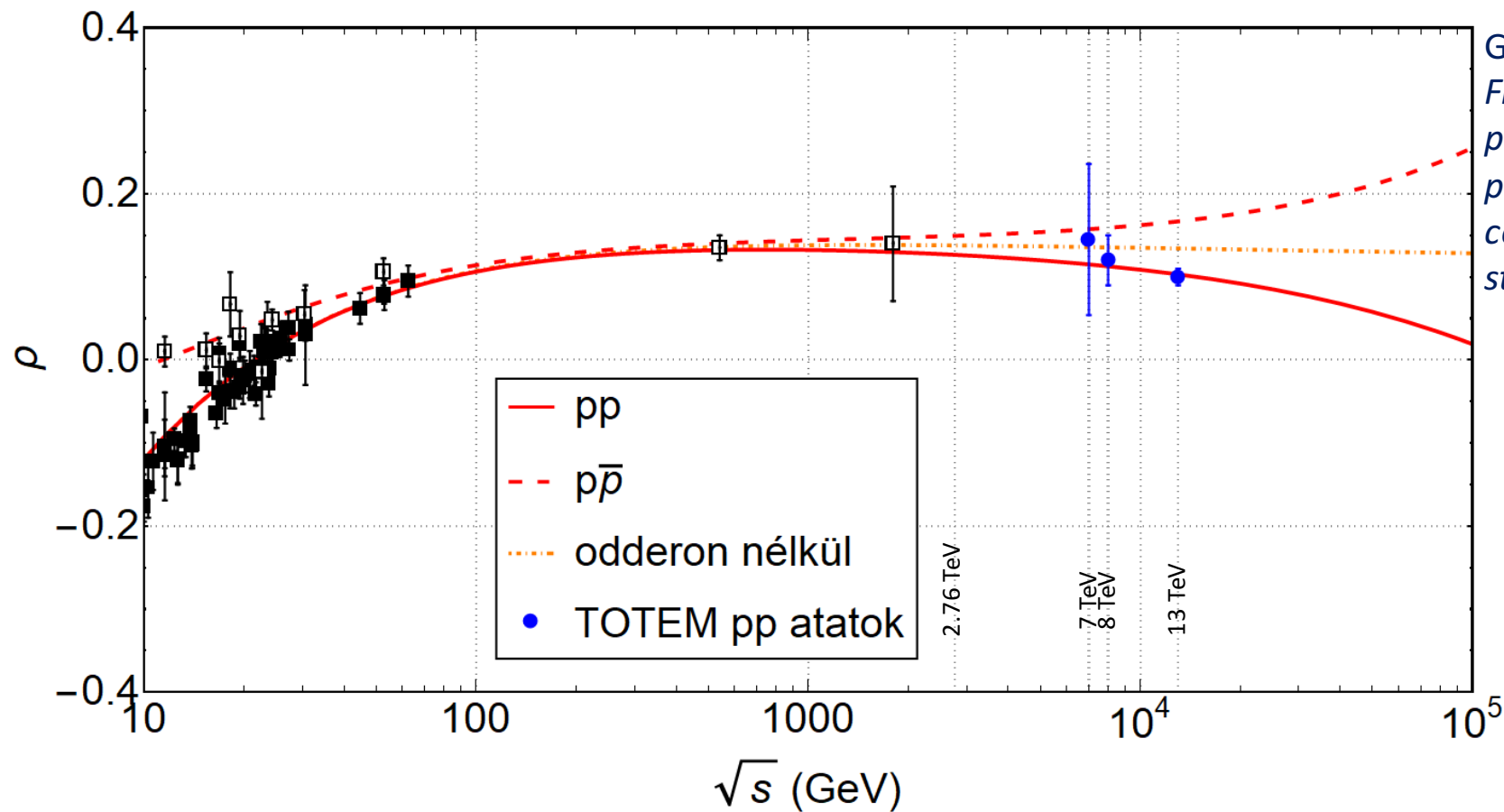


Fit to the differential cross section



The ratio ρ (phase)

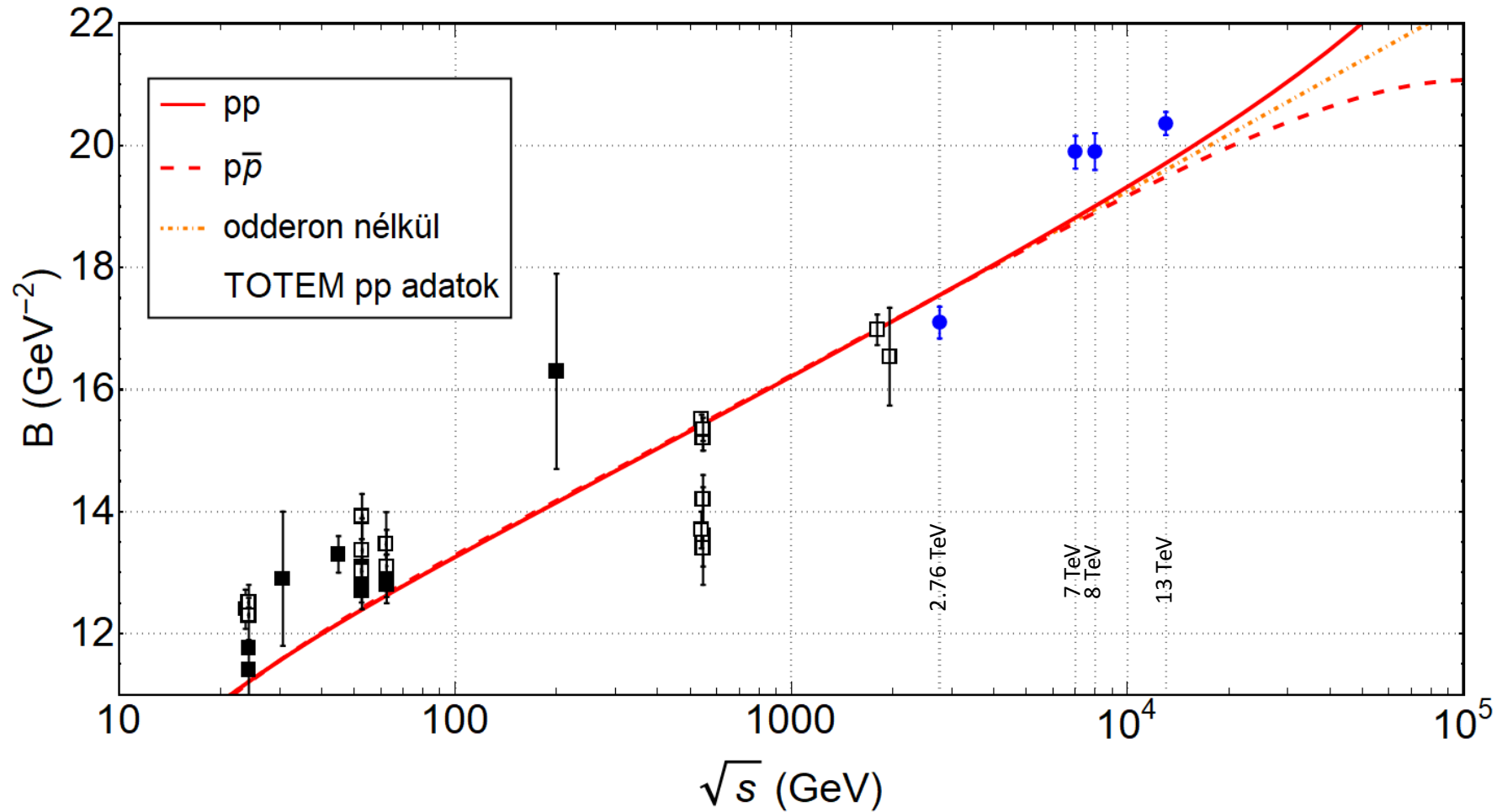
- $30 \leq \sqrt{s} \leq 13000$ GeV.



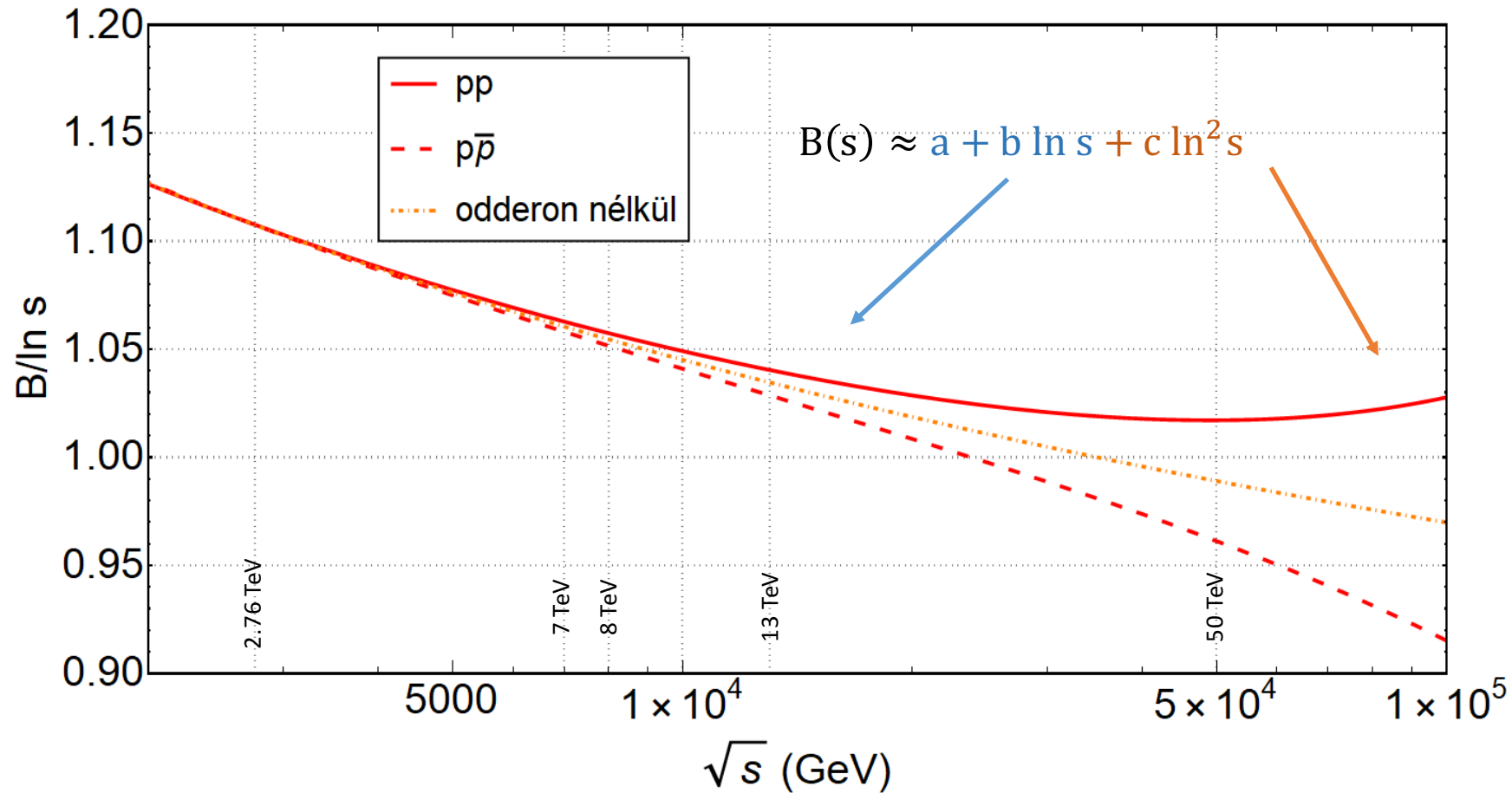
G. Antchev (TOTEM Collab.):
First determination of the ρ
parameter at $\sqrt{s} = 13$ TeV –
probing the existence of a
colourless three-gluon bound
state. [CERN-EP-2017-335](#)

Forward elastic slope $B(s)$

- $B(s) \sim \ln s \rightarrow \ln^2 s$?!



„Scaled”: $B(s)/\ln s$



Fitted values of the parameters

CERN ROOT MINUIT2 Migrad fit

Pomeron		Odderon		f- és ω -reggeon	
a_P	250 (rögzített)	a_O	0.115449 \pm 0.00304799	a_f	-13 (fixed)
b_P	14.7362 \pm 0.276352	b_O	0.711359 \pm 0.00201975	b_f	0 (fixed)
δ_P	0.0514965 \pm 0.000694922	δ_O	0.479593 \pm 0.00271713	s_{of}	1 (fixed)
α_{1P}	0.336121 \pm 0.00209166	α_{1O}	0.239799 \pm 0.0034584	a_ω	9 (fixed)
ϵ_P	0.0139516 \pm 0.000344159	ϵ_O	1.44154 \pm 0.0011131	b_ω	0 (fixed)
s_{0P}	100 (rögzített)	s_{0O}	100 (rögzített)	$s_{0\omega}$	1 (fixed)
NDF = 57		$\chi^2 = 49.2$		$\chi^2/\text{NDF} = 0.86$	

Local dispersion relations (Bronzan, Kane, Sukhatme, 1974);

$$\rho(s) = \frac{\text{Re}A(s,t=0)}{\text{Im}A(s,t=0)} = \frac{d \text{Ln } \sigma_{\text{tot}}(s)}{d \text{Ln } s}.$$

Hivatkozások

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THANK YOU !